

## Section 1.2 Functions and their properties

**Function:** is a rule that assigns one value of the dependent variable (output/y) for each value of the independent variable (input/x). “One y for each x”

**Recall vertical line test when looking at graphs**

**For equations pick x values to see if there is a unique output (only one answer)**

**Domain:** set of input values

**Range:** set of output values

**\*\*\*\*\*Give answers in interval notation!**

**Ex 1) Find the domain of each function**

a)  $f(x) = \sqrt{x+3}$

b)  $m(x) = \frac{x}{x-5}$

c)  $j(x) = \frac{\sqrt{x}}{x-5}$

d)  $g(x) = \sqrt{x-16}$

$$\mathbf{e)} \quad h(x) = \frac{x}{x^2 - 4}$$

$$\mathbf{f)} \quad c(x) = \frac{3x - 1}{(x + 3)(x - 1)}$$

$$\mathbf{g)} \quad k(x) = \sqrt{4 - x^2}$$

**Ex 2) Find the domain and the range of each function**

**(PICTURE IT!)**

$$\mathbf{a)} \quad f(x) = x^2 + 4$$

$$\mathbf{b)} \quad g(x) = 10 - x^2$$

**\*\* discuss 25,27 on HW Worksheet**

## (DAY 2)

**Vertical Asymptotes:** can be found by setting unique factors in denominator = 0

At vertical asymptotes, function outputs increase or decrease without bound

**Horizontal Asymptotes:** look at the graph on GC and trace out to very small and very large values of  $x$  (end behavior) to see if the outputs approach a value. OR know the rules:

- If Degree of Numerator = Degree of Denominator, then the HA is  $y = \text{ratio of leading coefficients}$
- If Degree of Numerator < Degree of Denominator, then the HA is  $y = 0$
- If Degree of Numerator > Degree of Denominator, then there is NO HA (there may be a slant asymptote)

**Ex 3) Find all horizontal and vertical asymptotes for each function.**

a)  $f(x) = \frac{x}{x^2 - 4}$

b)  $g(x) = \frac{3x - 1}{x + 3}$

**c)**  $h(x) = \frac{x+2}{3-x}$

**d)**  $p(x) = \frac{x}{x-1}$